



2011 Gordon Bell Awarded Peta-scale Applications

Peta-scale Phase-field Simulation for Dendritic Solidification

1 Phase-field Model

The mechanical properties of metal materials largely depend on their intrinsic internal microstructures. The phase-field simulation is the most powerful method known to simulate the micro-scale dendritic growth during solidification in a binary alloy. The phase-field model introduces a continuous order parameter (a phase-field variable) to describe whether the material is solid or liquid.

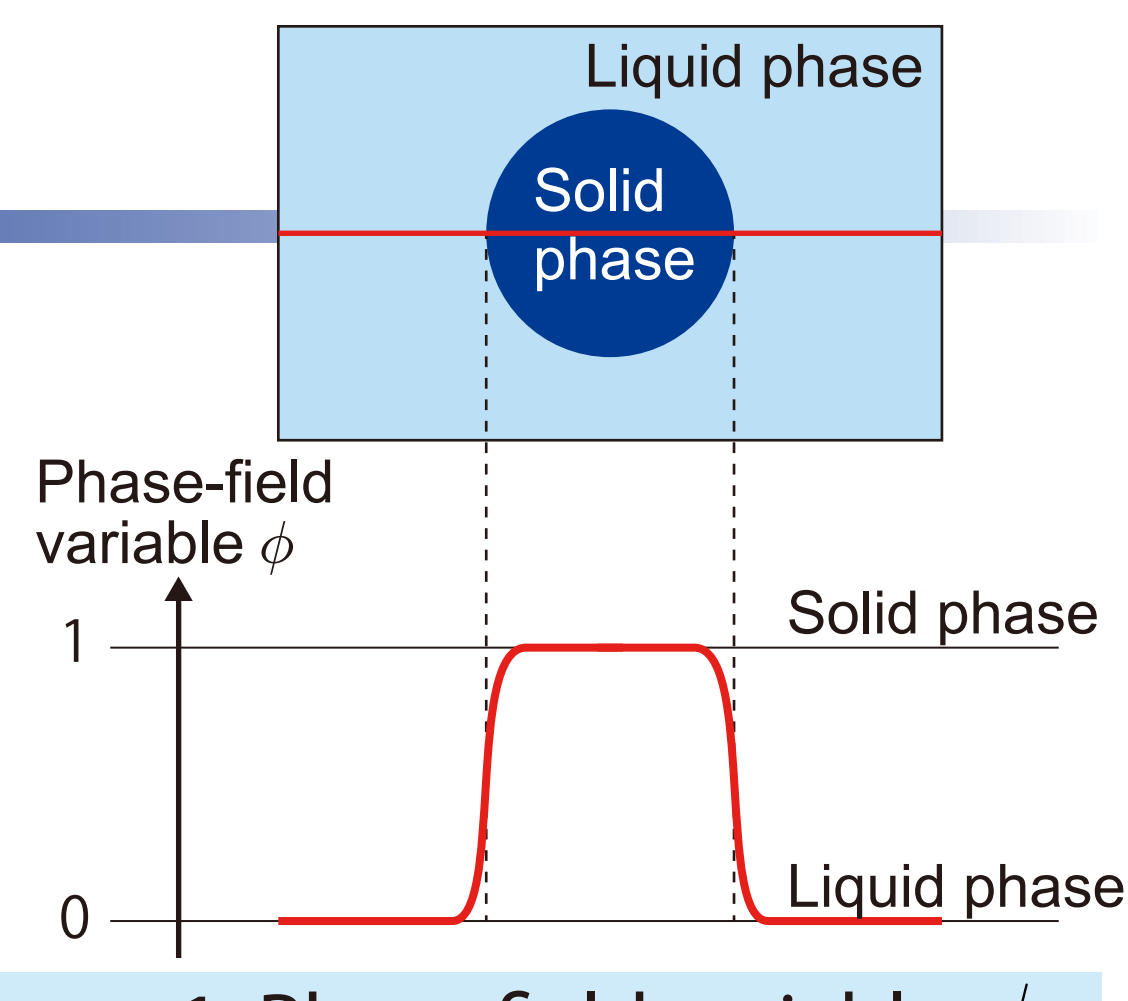


Figure 1: Phase-field variable ϕ

Governing equations

• Time integration of phase field (Allen-Cahn equation)

$$\frac{\partial \phi}{\partial t} = M_\phi \left[\nabla \cdot (a^2 \nabla \phi) + \frac{\partial}{\partial x} \left(a \frac{\partial a}{\partial \phi_x} |\nabla \phi|^2 \right) + \frac{\partial}{\partial y} \left(a \frac{\partial a}{\partial \phi_y} |\nabla \phi|^2 \right) + \frac{\partial}{\partial z} \left(a \frac{\partial a}{\partial \phi_z} |\nabla \phi|^2 \right) - \Delta S \Delta T \frac{d\phi}{d\phi} - W \frac{d\phi}{d\phi} \right]$$

• Time integration of solute concentration

$$\frac{\partial c}{\partial t} = \nabla \cdot [D_S \phi \nabla c_S + D_L (1 - \phi) \nabla c_L]$$

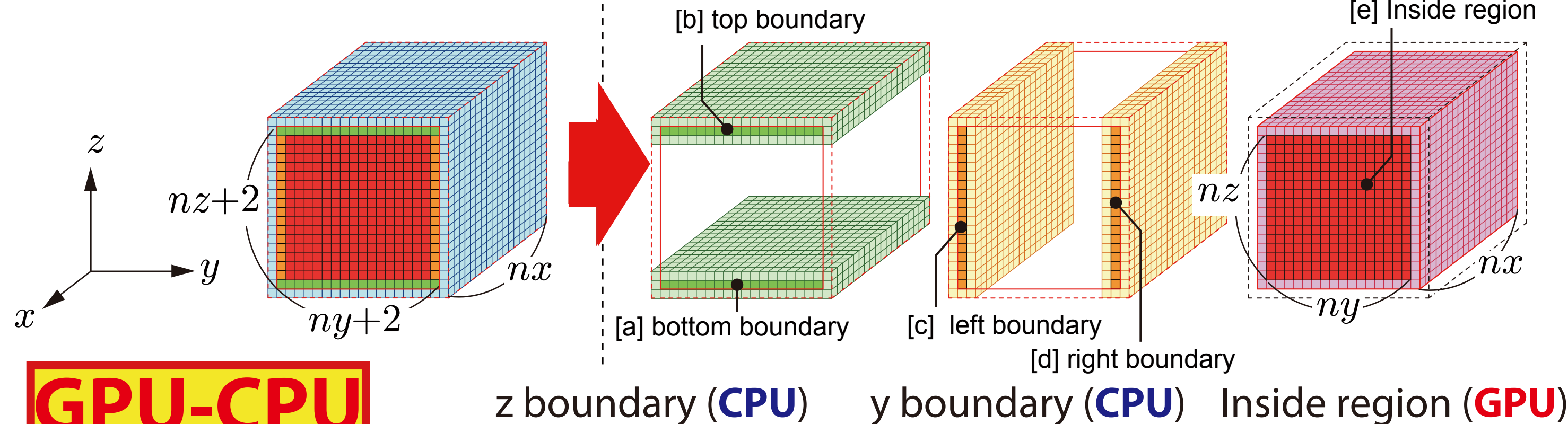
$$c_S = \frac{kc}{1 - \phi + k\phi}, c_L = \frac{c}{1 - \phi + k\phi}, k = c_S/c_L \quad D_S: \text{Diffusion coefficient in solid phase} \quad D_L: \text{Diffusion coefficient in liquid phase}$$

M_ϕ : Mobility
 a : Anisotropy
 ΔS : Entropy of fusion
 ΔT : Undercooling
 $p(\phi) = \phi^3(10 - 15\phi + 6\phi^2)$
 $q(\phi) = \phi^2(1 - \phi)^2$

Implementation

Whole subdomain Divided domains

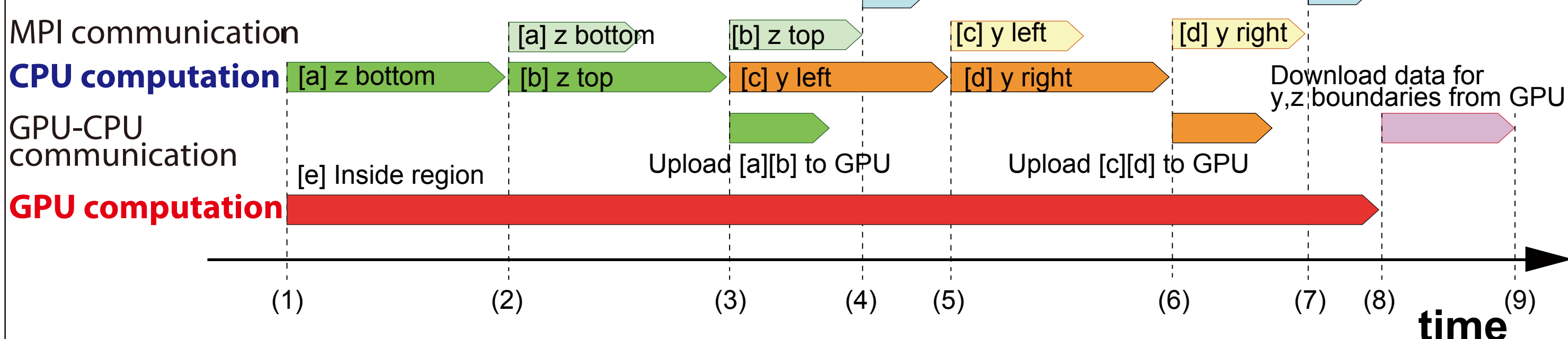
Figure 2: Scheme of the Hybrid-YZ method



GPU-CPU Hybrid

z boundary (CPU) y boundary (CPU) Inside region (GPU)

Copy corners of z boundary to y boundary Copy corners of y boundary to z boundary



ACM Gordon Bell Prize
Special Achievements in Scalability and Time-to-Solution
& SC'11 Technical Paper

"Peta-scale Phase-Field Simulation for Dendritic Solidification on the TSUBAME 2.0 Supercomputer"

T. Shimokawabe, T. Aoki, T. Takaki, A. Yamanaka, A. Nukada, T. Endo, N. Maruyama, and S. Matsuoka,

2 Simulation using TSUBAME 2.0

2.000 PFlops!!! on 4000 GPUs with 16000 CPU cores

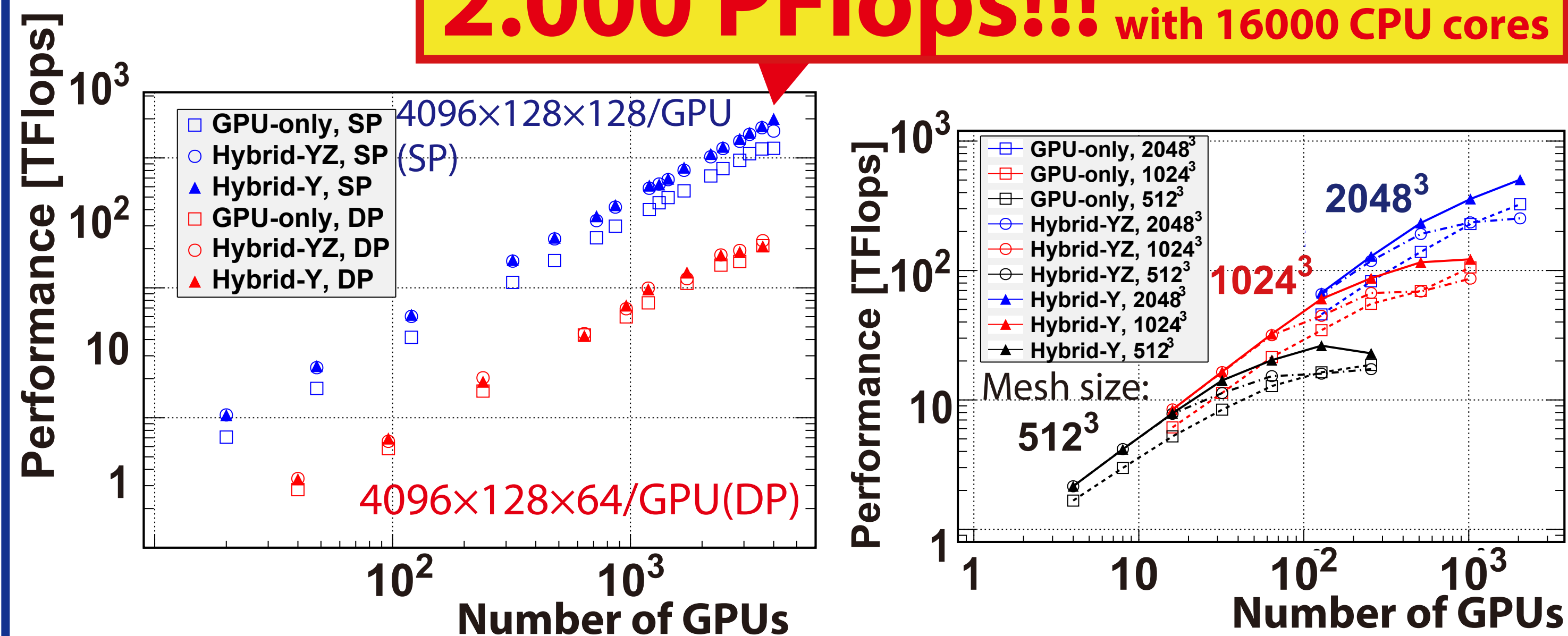
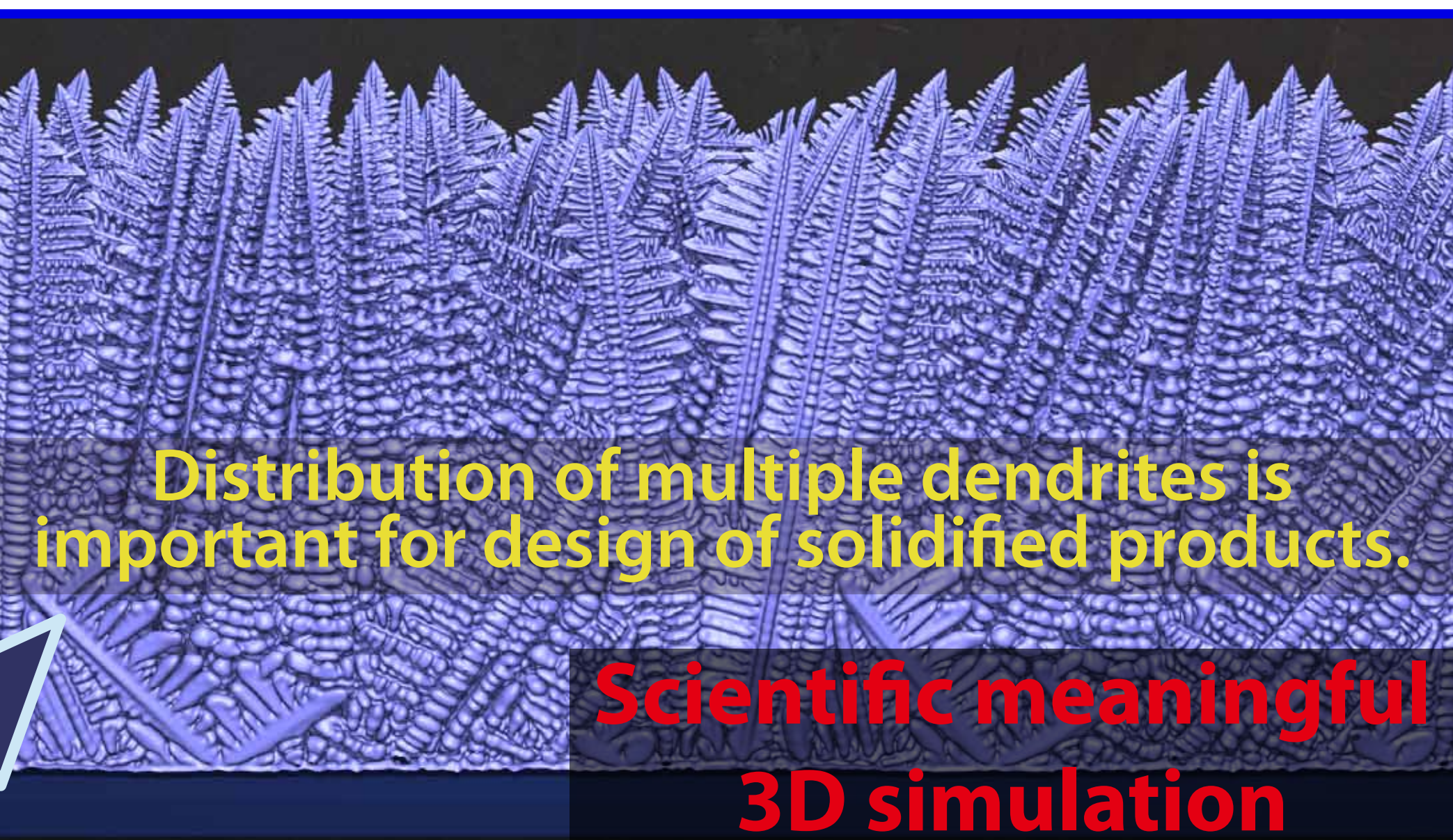


Figure 3: Weak scaling results

Figure 4: Strong scaling results

Figure 5: Dendritic growth in the binary alloy solidification with $4096 \times 1024 \times 4096$ mesh with 768 GPUs of TSUBAME2.0



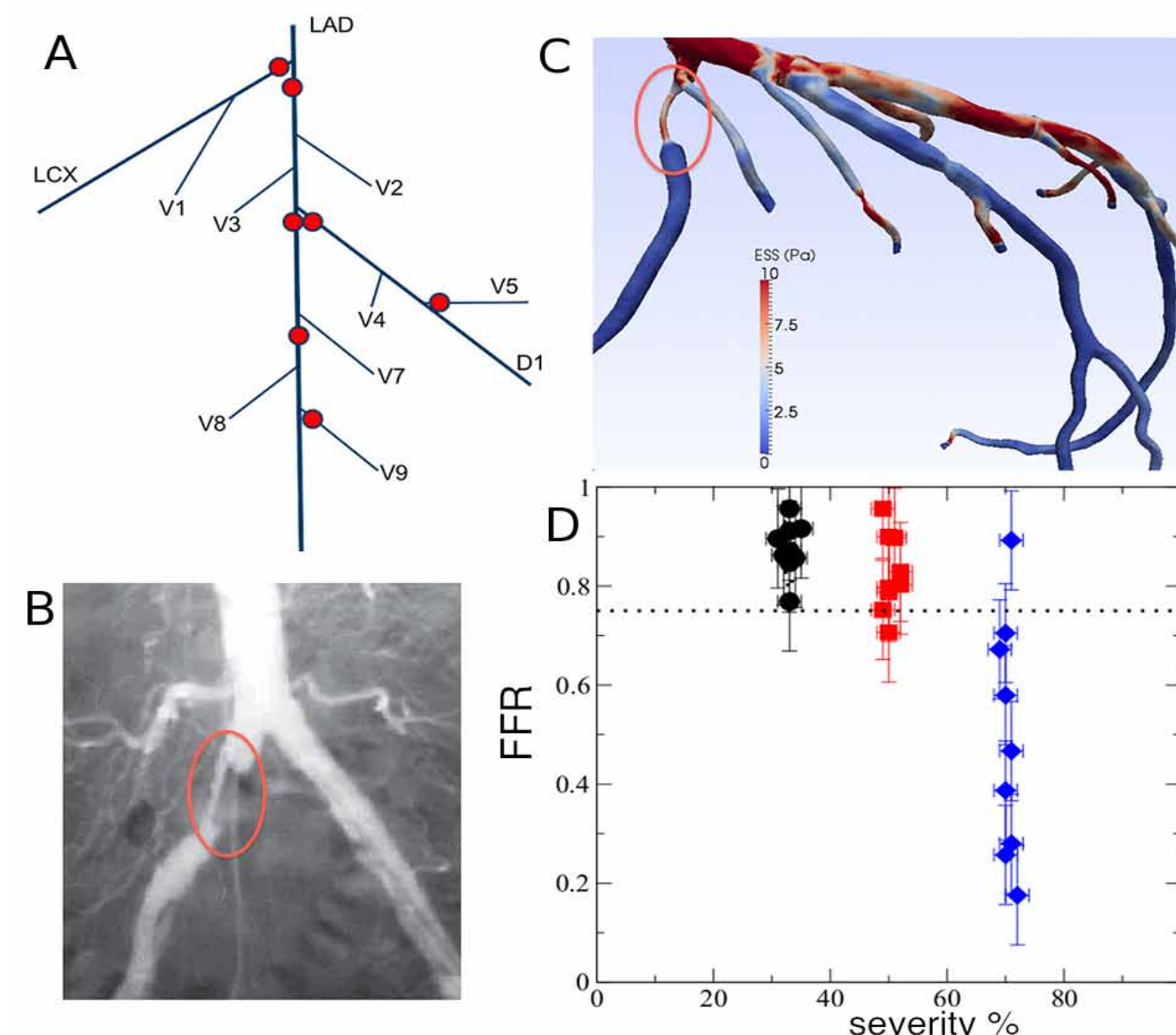
Initial condition

~ mm

Petaflop Biofluidics Simulations on a Two-Million Core System

Multiscale Computational Hemodynamics

Clinical guidance for determining dangerous plaques



Time to completion is crucial for clinical intervention

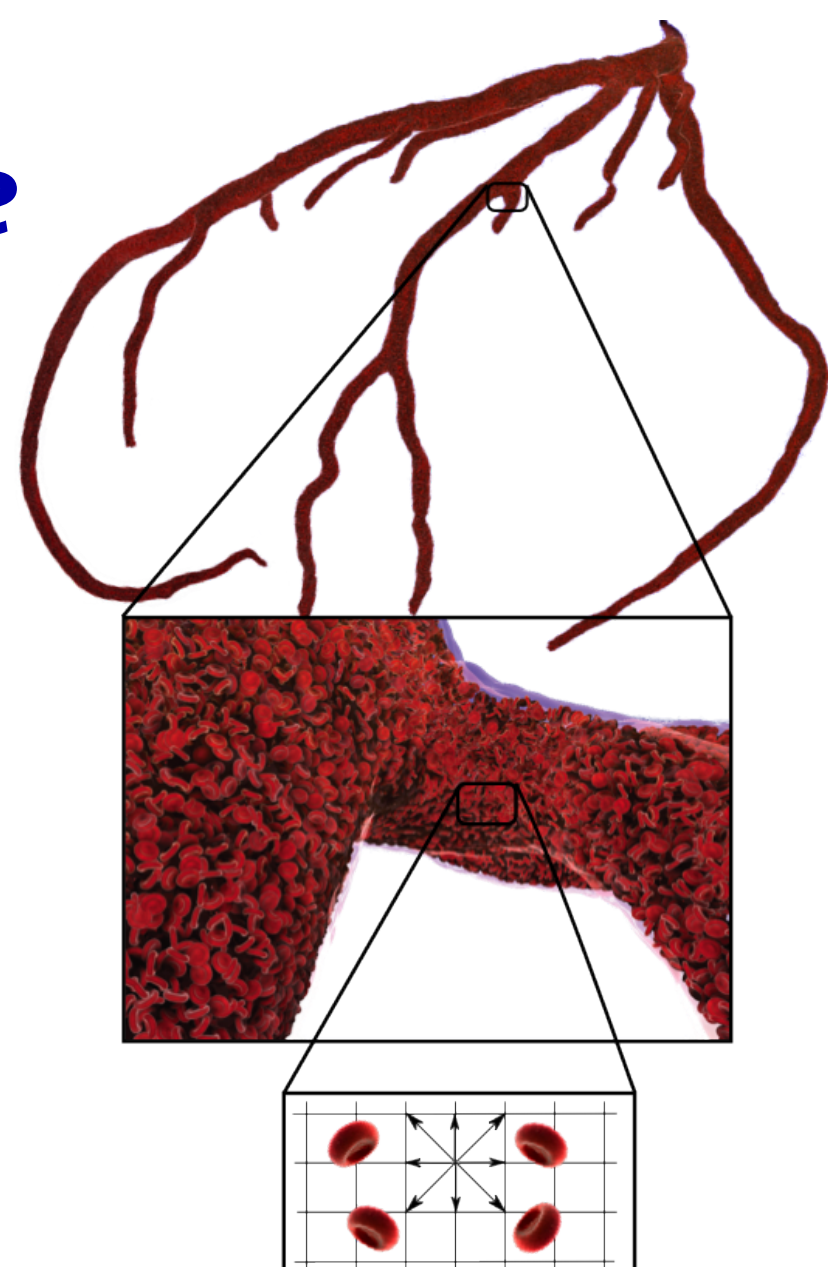
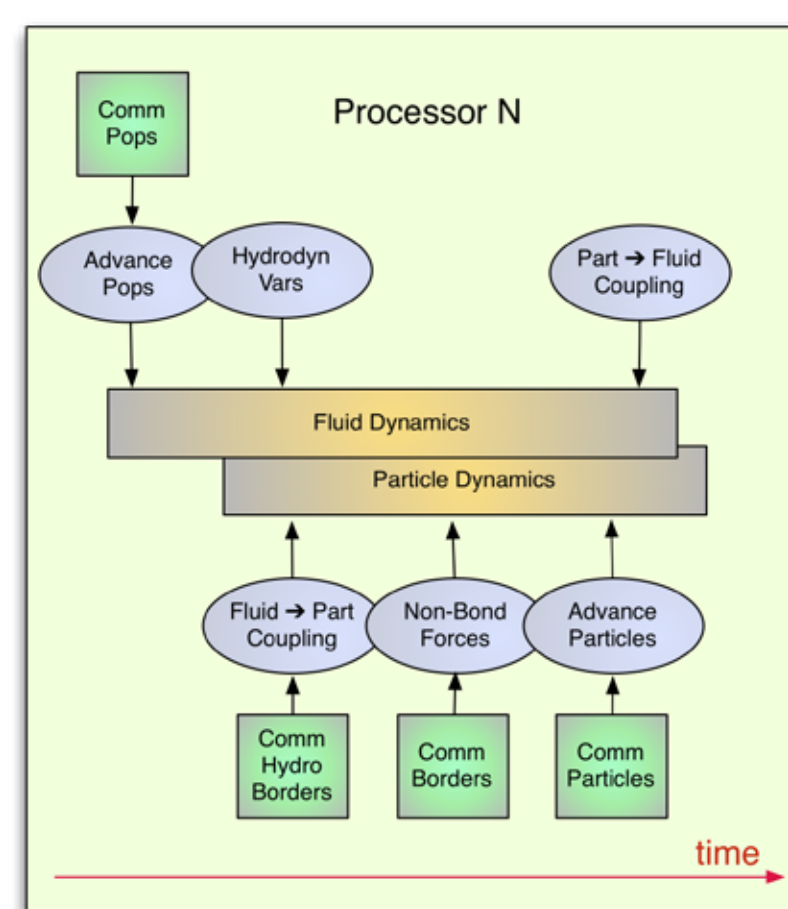
HPC is mandatory

The MUPHY code for Multiscale Hemodynamics

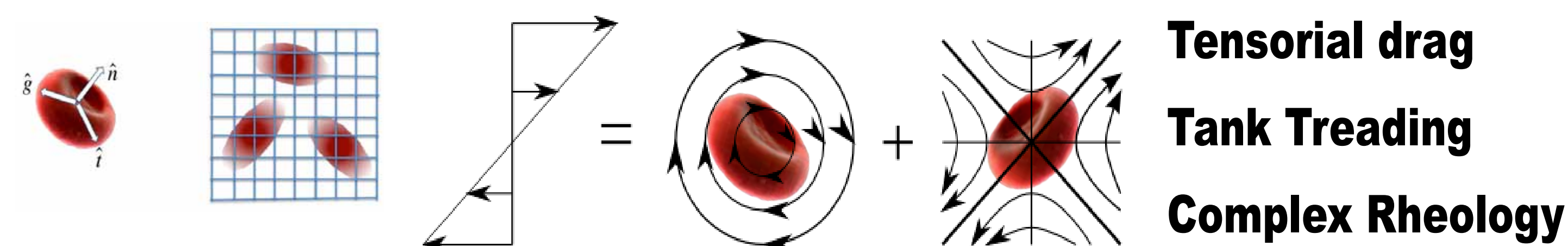
Blood Plasma:
Lattice Boltzmann Method

coupled

Red Blood Cells:
Molecular Dynamics

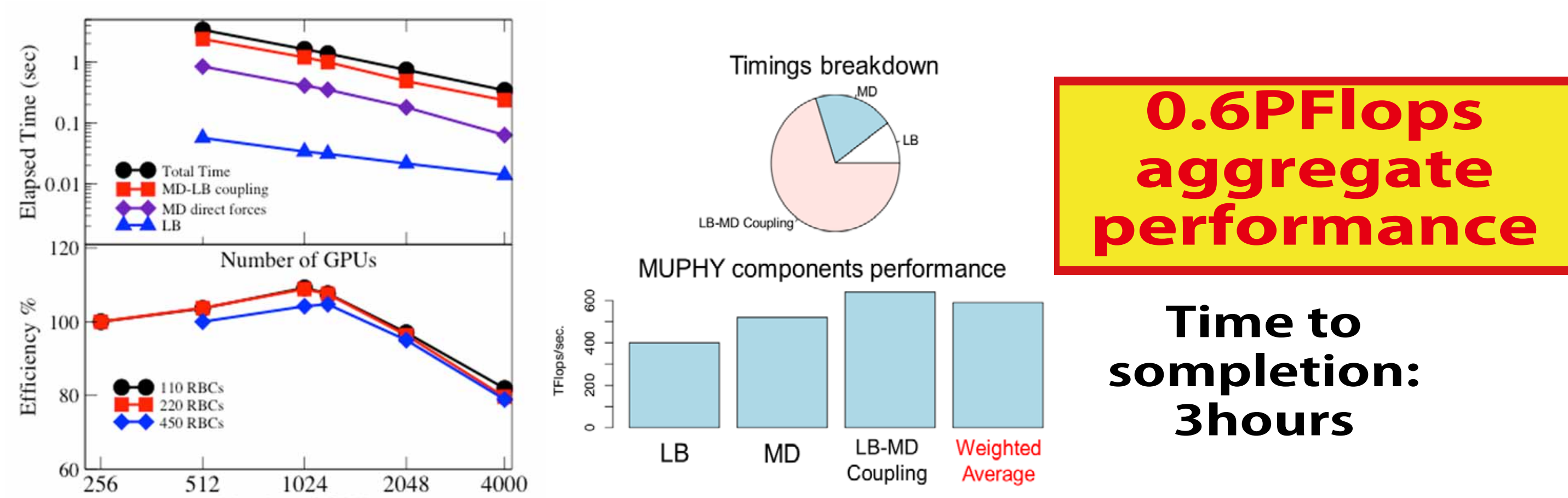


Hydrodynamic Coupling



- Strip off degrees of freedom: $O(10)$ per Red Blood Cell
- Complex boundaries via local collisions (no Green's function)

Performance on 4000GPUs of TSUBAME 2.0



0.6PFlops aggregate performance

Time to completion:
3 hours



2011 ACM Gordon Bell Prize Honorable Mention
"Petaflop Biofluidics Simulations On A Two Million-Core System"

Massimo Bernaschi, Mauro Bisson, Toshio Endo, Massimiliano Fatica, Satoshi Matsuoka, Simone Melchionna, Sauro Succi

Collaborative work with IAC-CNR, Italy, NVIDIA and Harvard University

