



# 2011 Gordon Bell Awarded Peta-scale Applications

## Peta-scale Phase-field Simulation for Dendritic Solidification

### 1 Phase-field Model

The mechanical properties of metal materials largely depend on their intrinsic internal microstructures. The phase-field simulation is the most powerful method known to simulate the micro-scale dendritic growth during solidification in a binary alloy. The phase-field model introduces a continuous order parameter (a phase-field variable) to describe whether the material is solid or liquid.

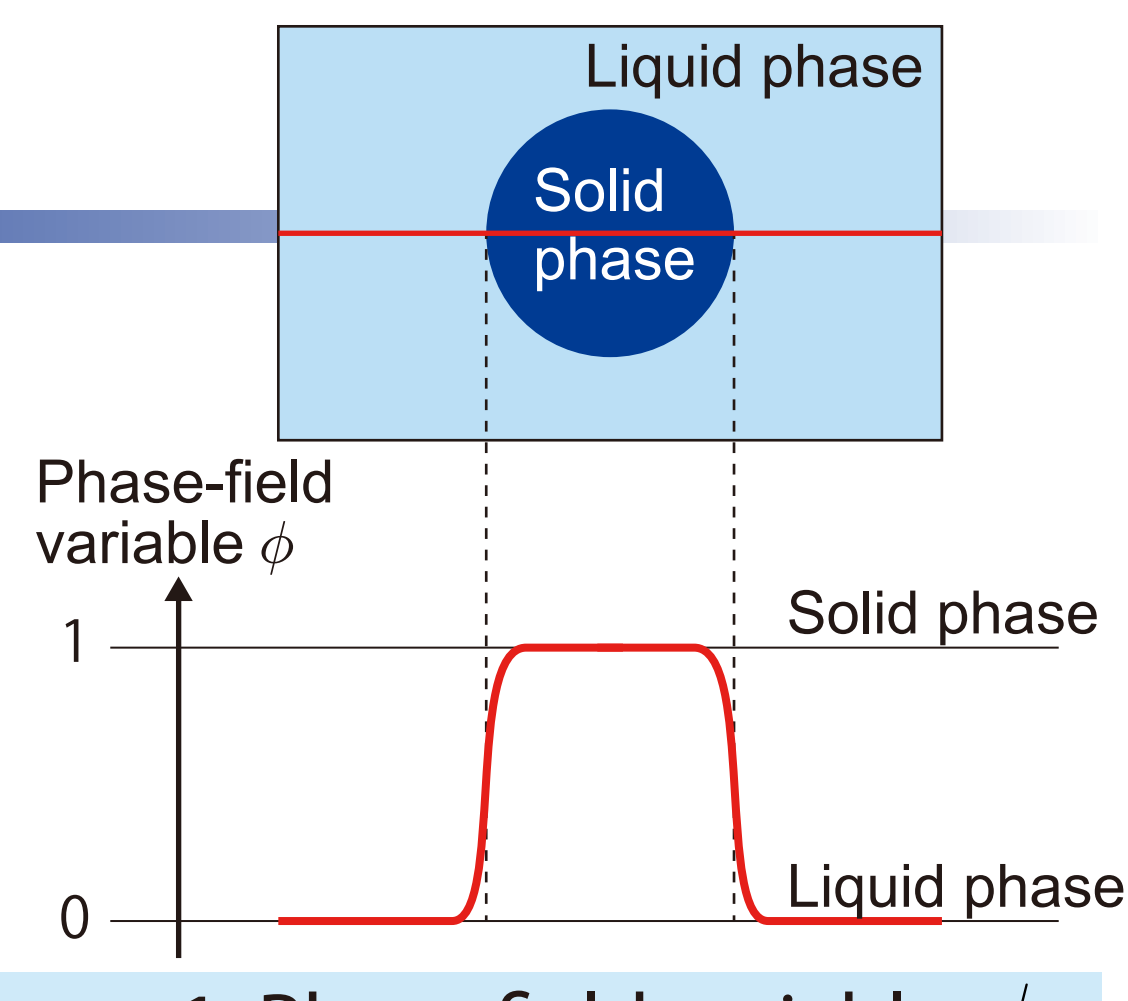


Figure 1: Phase-field variable  $\phi$

### Governing equations

• Time integration of phase field (Allen-Cahn equation)

$$\frac{\partial \phi}{\partial t} = M_{\phi} \left[ \nabla \cdot (a^2 \nabla \phi) + \frac{\partial}{\partial x} \left( a \frac{\partial a}{\partial \phi_x} |\nabla \phi|^2 \right) + \frac{\partial}{\partial y} \left( a \frac{\partial a}{\partial \phi_y} |\nabla \phi|^2 \right) + \frac{\partial}{\partial z} \left( a \frac{\partial a}{\partial \phi_z} |\nabla \phi|^2 \right) - \Delta S \Delta T \frac{d\phi}{d\phi} - W \frac{d\phi}{d\phi} \right]$$

• Time integration of solute concentration

$$\frac{\partial c}{\partial t} = \nabla \cdot [D_S \phi \nabla c_S + D_L (1 - \phi) \nabla c_L]$$

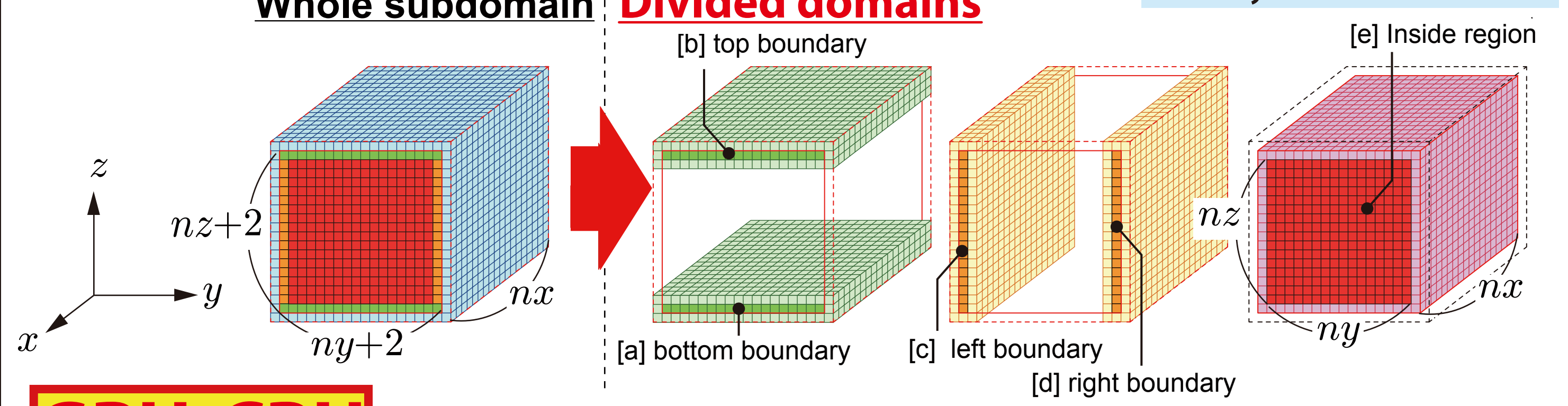
$$c_S = \frac{kc}{1 - \phi + k\phi}, \quad c_L = \frac{c}{1 - \phi + k\phi}, \quad k = c_S / c_L \quad D_S: \text{Diffusion coefficient in solid phase} \quad D_L: \text{Diffusion coefficient in liquid phase}$$

$M_{\phi}$ : Mobility  
 $a$ : Anisotropy  
 $\Delta S$ : Entropy of fusion  
 $\Delta T$ : Undercooling  
 $p(\phi) = \phi^3(10 - 15\phi + 6\phi^2)$   
 $q(\phi) = \phi^2(1 - \phi)^2$

### Implementation

Whole subdomain    Divided domains

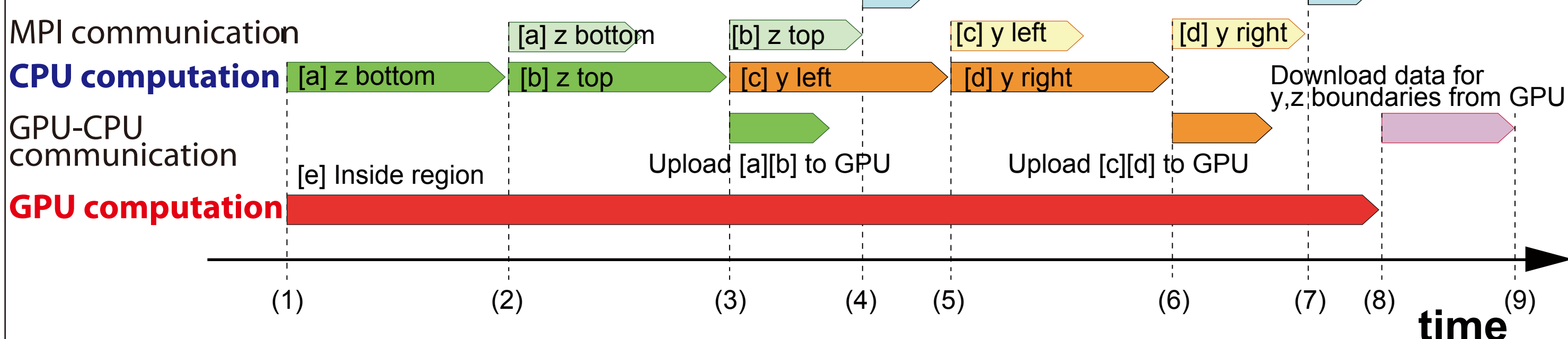
Figure 2: Scheme of the Hybrid-YZ method



**GPU-CPU Hybrid**

z boundary (CPU)    y boundary (CPU)    Inside region (GPU)

Copy corners of z boundary to y boundary    Copy corners of y boundary to z boundary



ACM Gordon Bell Prize  
Special Achievements in Scalability and Time-to-Solution  
& SC'11 Technical Paper

"Peta-scale Phase-Field Simulation for Dendritic Solidification on the TSUBAME 2.0 Supercomputer"

T. Shimokawabe, T. Aoki, T. Takaki, A. Yamanaka, A. Nukada, T. Endo, N. Maruyama, and S. Matsuoka,

### 2 Simulation using TSUBAME 2.0

**2.000 PFlops!!!** on 4000 GPUs with 16000 CPU cores

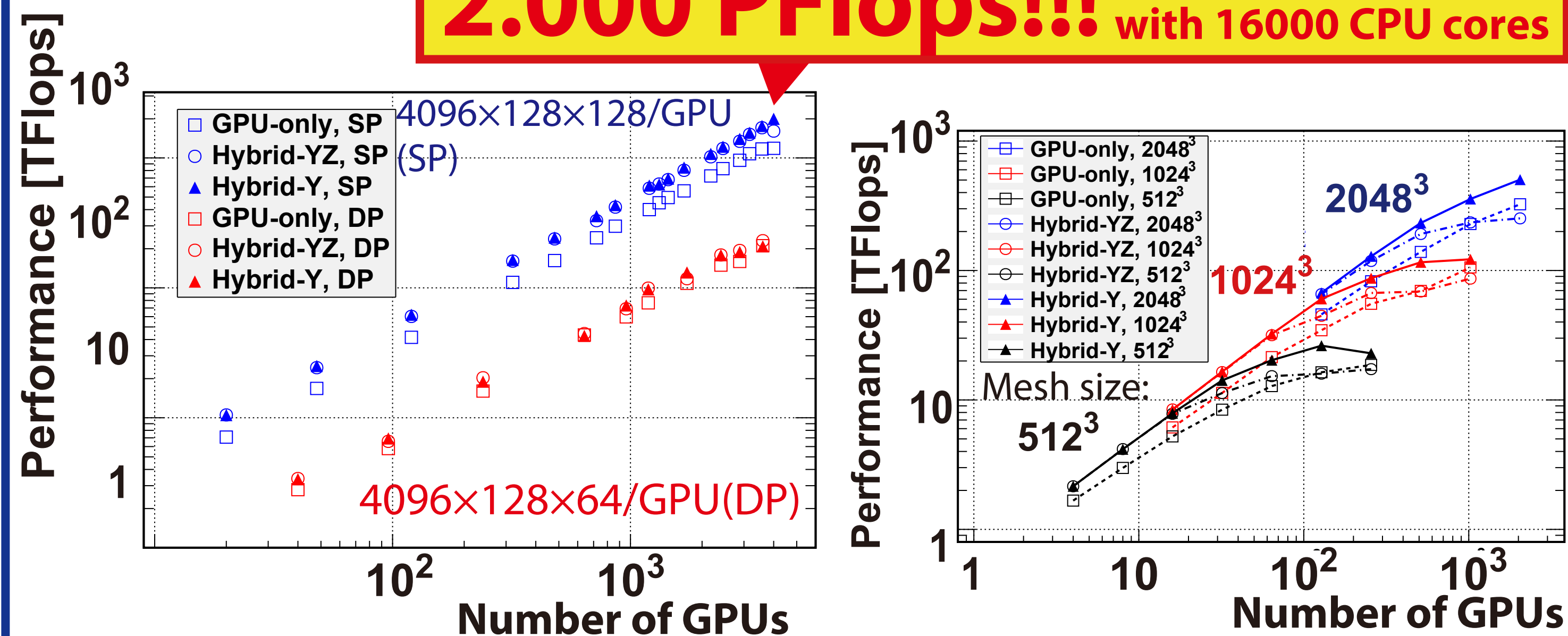
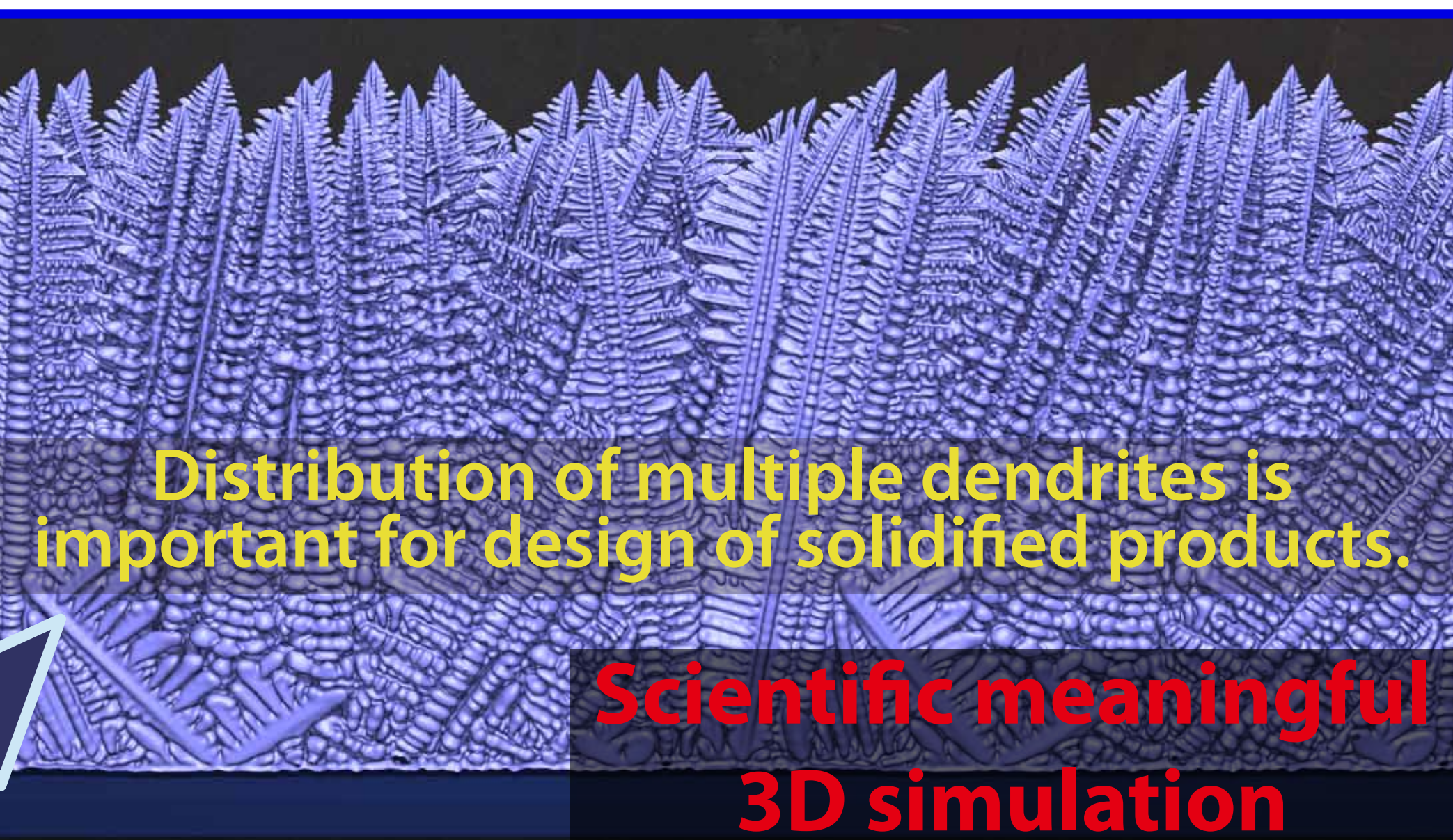


Figure 3: Weak scaling results

Figure 4: Strong scaling results

Figure 5: Dendritic growth in the binary alloy solidification with  $4096 \times 1024 \times 4096$  mesh with 768 GPUs of TSUBAME2.0



Initial condition

Distribution of multiple dendrites is important for design of solidified products.

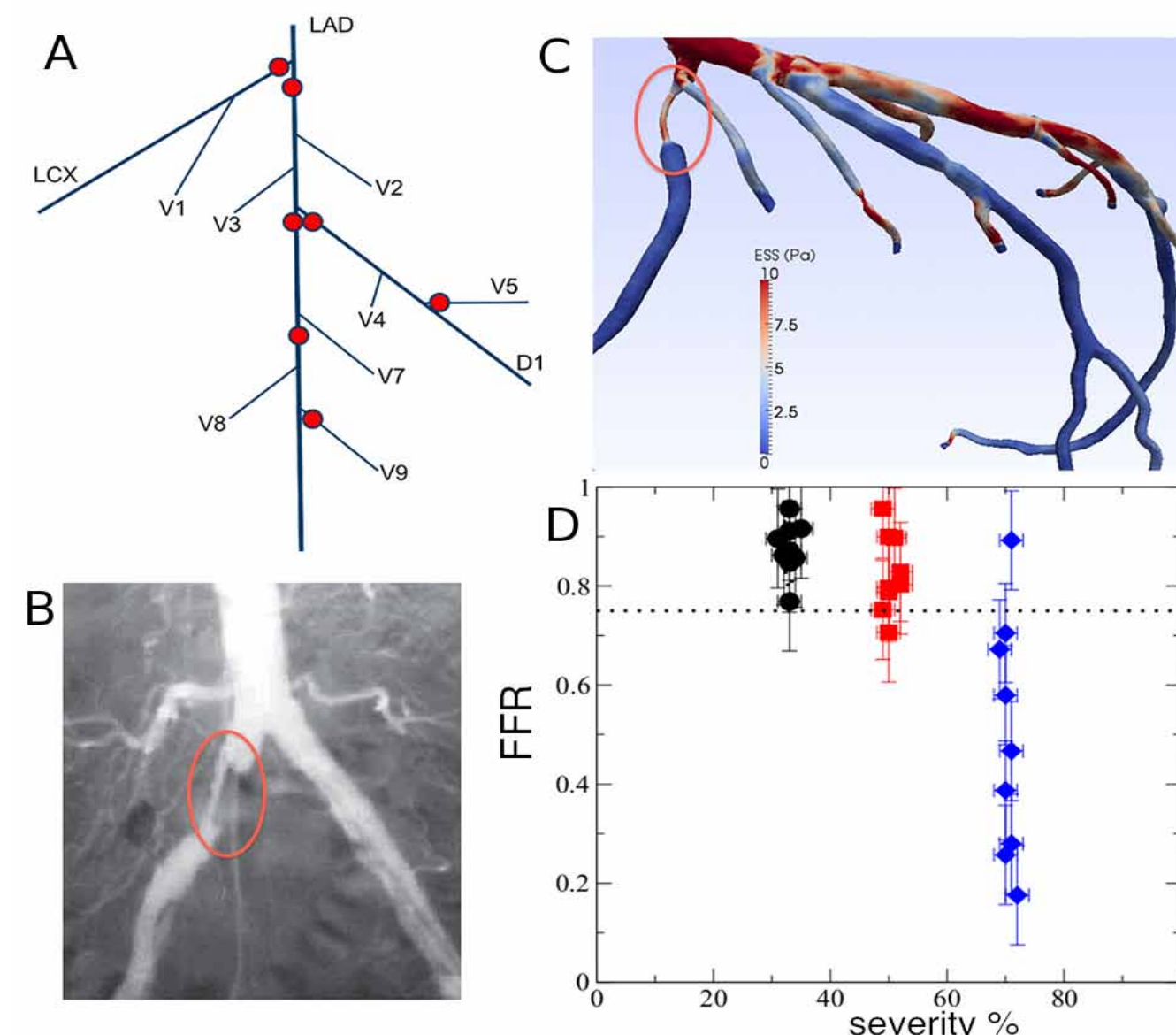
Scientific meaningful 3D simulation



## Petaflop Biofluidics Simulations on a Two-Million Core System

### Multiscale Computational Hemodynamics

Clinical guidance for determining dangerous plaques

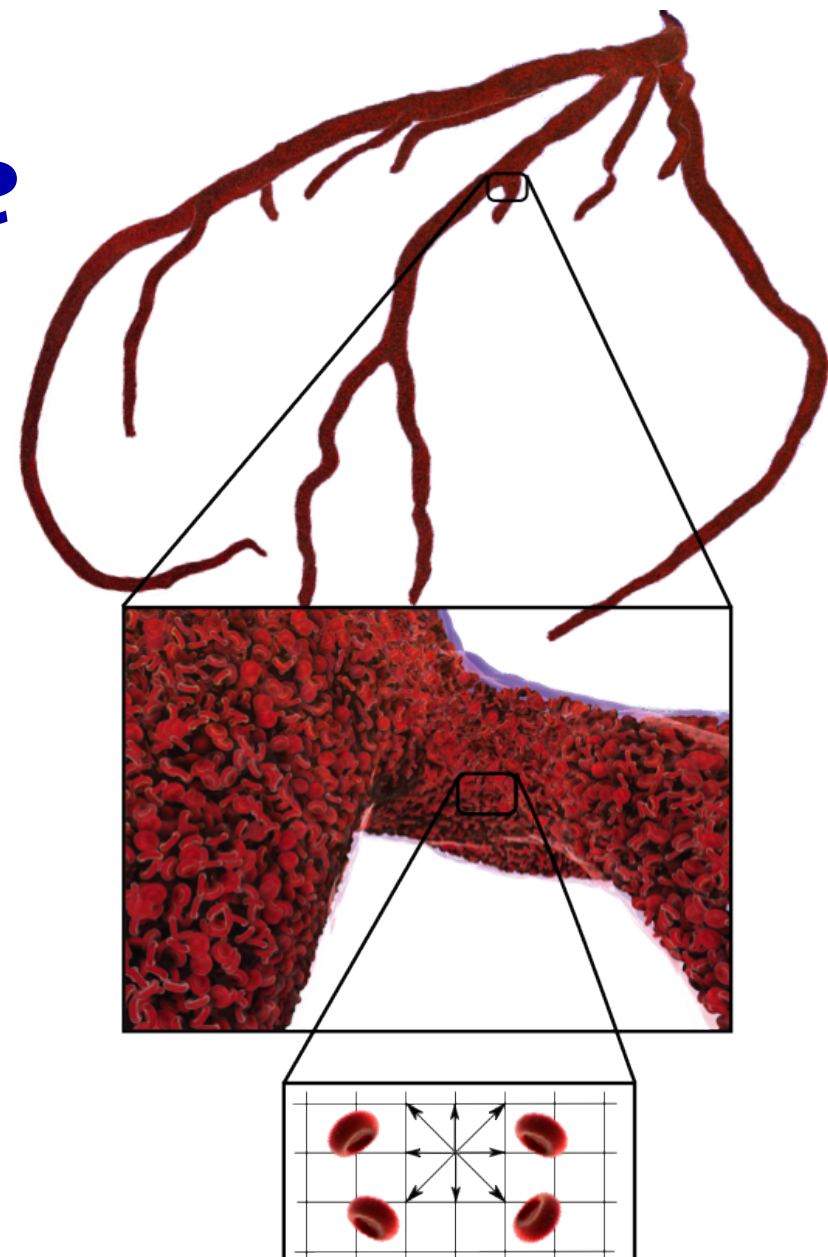
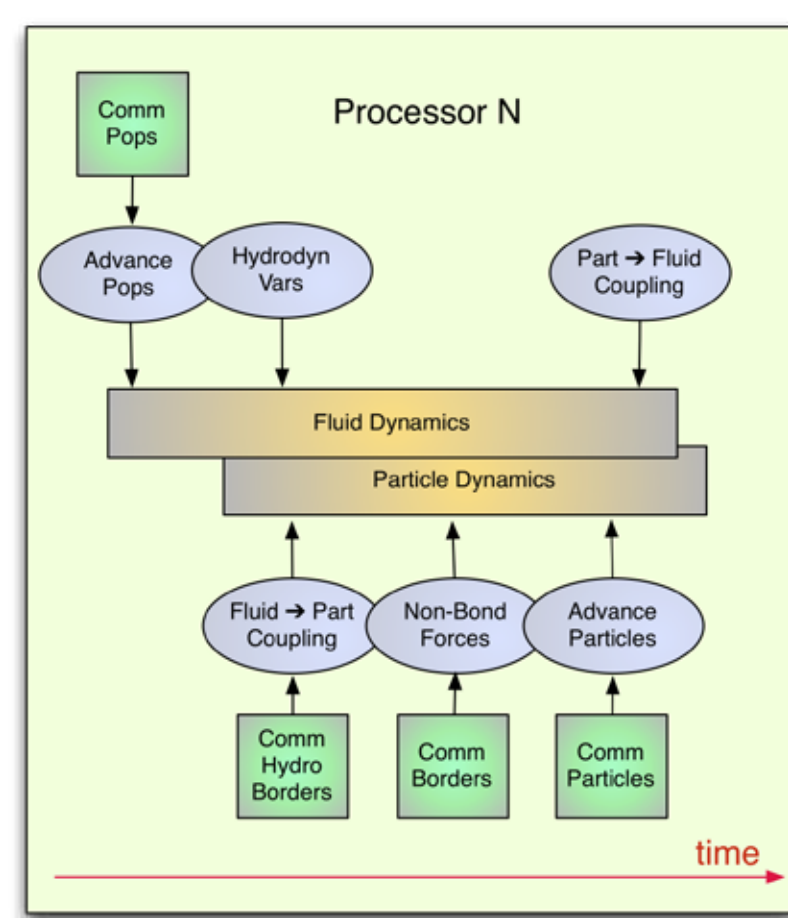


Time to completion is crucial for clinical intervention

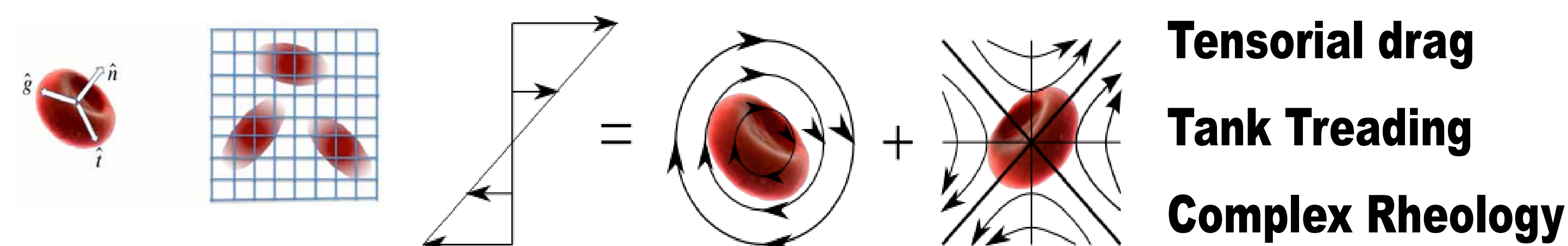
HPC is mandatory

### The MUPHY code for Multiscale Hemodynamics

Blood Plasma:  
Lattice Boltzmann Method  
↕ coupled  
Red Blood Cells:  
Molecular Dynamics

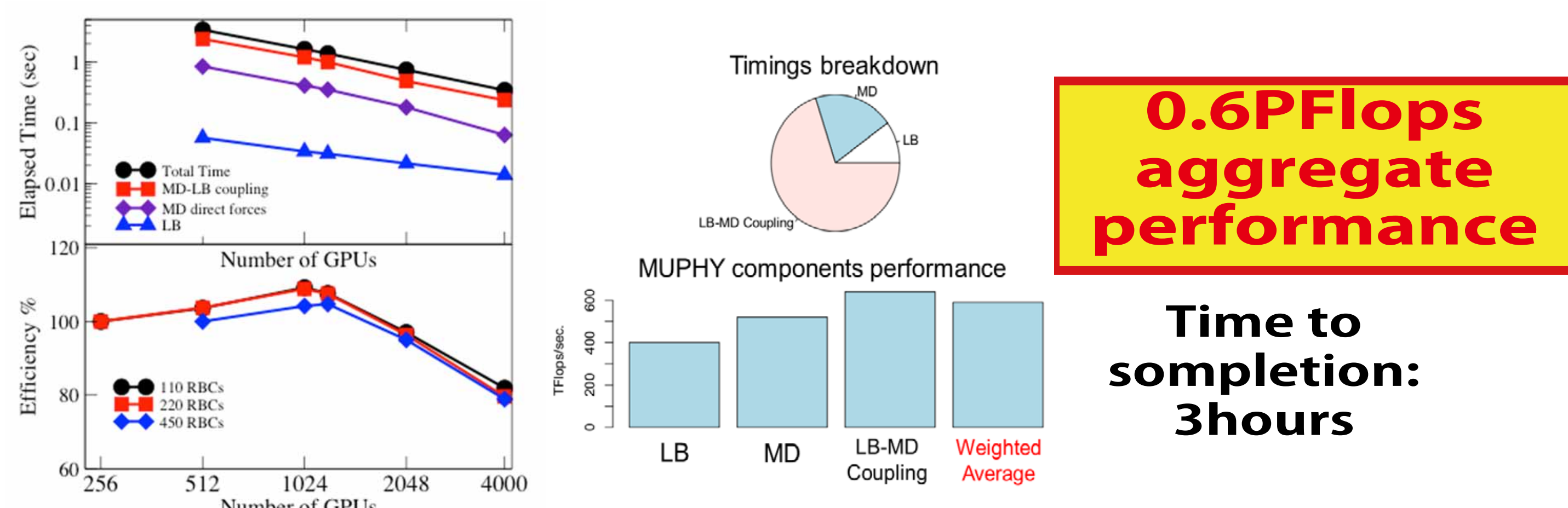


### Hydrodynamic Coupling



- Strip off degrees of freedom:  $O(10)$  per Red Blood Cell
- Complex boundaries via local collisions (no Green's function)

### Performance on 4000GPUs of TSUBAME 2.0



2011 ACM Gordon Bell Prize Honorable Mention  
"Petaflop Biofluidics Simulations On A Two Million-Core System"

Massimo Bernaschi, Mauro Bisson, Toshio Endo, Massimiliano Fatica, Satoshi Matsuoka, Simone Melchionna, Sauro Succi

Collaborative work with IAC-CNR, Italy, NVIDIA and Harvard University

